

Numerical Analysis of Supercontinuum Generated Micro-structured Optical Fiber with all Normal Chromatic Dispersion

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Abstract: A micro-structured photonic crystal fiber (M-PCF) with all normal chromatic dispersion has been proposed for supercontinuum spectrum generation which is applicable in optical transmission and optical coherence tomography applications. Calculations of its different properties using finite difference method have shown that the proposed M-PCF has a high nonlinear coefficients at 1.06 μm , 1.30 μm and 1.55 μm wavelength with flattened chromatic dispersion, low confinement losses and broad supercontinuum spectrum. Moreover, it has been shown that the proposed design obtain high power and short fiber length at 1.06 μm , 1.30 and 1.55 μm center wavelengths by propagating sech^2 picosecond optical pulses with 1.0 ps pulse width at a full width at half maximum.

Key words: *Microstructured fiber, chromatic dispersion, supercontinuum spectrum, longitudinal resolution*

INTRODUCTION

Micro-structured fiber, also called photonic crystal fiber (PCF), has attracted considerable attention from the optical community due to its remarkable dispersion and leakage properties [1, 2]. PCF has a large refractive index difference between its core and its effective cladding; and as a result, most of the energy of the fundamental mode is distributed within the core region. With light concentrated on a smaller area at a higher intensity, PCF can dramatically lower the thresholds of nonlinear optical effects.

Liao et al. [3] presented two highly nonlinear PCFs with nonlinear coefficients of $22.83 \text{ W}^{-1}\text{km}^{-1}$ and $29.65 \text{ W}^{-1}\text{km}^{-1}$ at the 1.55 μm wavelength. The designed structures contain four different air hole diameters with hybrid claddings air holes arrangement. Doped PCF structure with nonlinear coefficients of $31.5 \text{ W}^{-1}\text{km}^{-1}$ and $36.5 \text{ W}^{-1}\text{km}^{-1}$ at the 1.55 μm wavelength, were presented by Xu et al. [4] and Matloub et al. [5], respectively. A modified hexagonal index guiding photonic crystal fiber with an even higher nonlinear coefficient of $37.1 \text{ W}^{-1}\text{km}^{-1}$ at the 1.55 μm wavelength was presented by Hao et al. [2]. Despite the reasonably high nonlinear coefficients,

their designs are difficult to fabricate; either due to the multiple air hole diameters [3], doped nature of the fiber [4, 5] or the presence of multiple core in the designs [2]. Additionally, nonlinear coefficients of these fibers shall be shown to be lower than that of our proposed design. Other non-hexagonal arrangements of air holes, such as square lattice structure [6], have also been proposed in the literature.

High nonlinear coefficient is also crucial for the generation of supercontinuum (SC) spectrum. Till now, super-luminescent diodes (SLDs) [7, 8], femtosecond pulse laser sources [9-12] and picosecond pulse laser source [13] have been investigated as broadband light sources. Generation of SC spectrum with 80 nm bandwidth and 2 mW to 15 mW output power centered at approximately 1.2 μm wavelength have been demonstrated by Shibita et al. [7]. Bayleyegn et al. [8] produced an SC spectrum with 200 nm full width at half maxima and 10 mW source output power centered at 1.3 μm wavelength. These output powers are, however, insufficient for the identification of individual cells [7]. Furthermore, multiplexed SLD light sources were used; with complex designs but low output power [8]. Zaytsev et al. [9] reported an SC spectrum pumped with 200 fs Yb-doped fiber laser at

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central wavelength of 1.07 μm , to obtain 11 nm spectrum FWHM and 800 mW output power. Karim et al. [10] and Ahmad et al. [11] demonstrated the use of 1 kW and 100 W input peak power to generate SC spectrum at 1.55 μm centre wavelength, with chalcogenide glass core. In reference [12], input peak power of 1.38 kW has been used to generate SC spectra at centre wavelength of 1.3 μm and 1.65 μm . However, femtosecond pulse light sources are generally more expensive as compared to picosecond pulse light sources, with picosecond pulse light sources having better properties as compared to both femtosecond pulse light source and SLDs. A highly nonlinear photonic crystal fiber in OCT as a picosecond pulse laser source, is presented in reference [13]. Consequently, this paper proposes an M-PCF as a picosecond pulse laser source, due to the benefits associated with picosecond pulse laser source.

In this paper, a seven-ring M-PCF structure is proposed for supercontinuum generation with all normal chromatic dispersion. Numerical simulation results have shown that the proposed M-PCF has a high nonlinear coefficients of more than $104 \text{ W}^{-1}\text{km}^{-1}$, $72 \text{ W}^{-1}\text{km}^{-1}$ and $52 \text{ W}^{-1}\text{km}^{-1}$ at wavelengths 1.06 μm , 1.30 μm and 1.55 μm respectively, with a very low confinement loss of less than 10^{-2} dB/km in the 1.05 to 1.65 wavelength ranges. Moreover, the proposed M-PCF exhibits an ultra-flattened chromatic dispersion of $0.0 \sim -4.5 \text{ ps}/(\text{nm}\cdot\text{km})$ and broad supercontinuum spectrum in the targeted wavelength range, making it suitable for optical transmissions and SC generation applications. The proposed M-PCF also exhibits high power and short fiber length at center wavelength 1.06 μm , 1.30 μm and 1.55 μm , which are superior to that in references [7-13].

NUMERICAL SIMULATION METHODS

Full vector finite difference method with anisotropic perfectly matched layer was used to calculate different properties of the proposed M-PCF. Chromatic dispersion D , chromatic dispersion slope D_s , confinement loss L_c , effective area A_{eff} , and nonlinear coefficient γ , were some of the important parameters considered and calculated using equations (1)-(5) [6, 13, 14]. Material dispersion, given by Sellmeier equation, has been directly included in the calculation and as such, chromatic dispersion corresponds to total dispersion of the M-PCF [6, 13, 14].

$$D(\lambda) = -\frac{\lambda}{c} \frac{\partial^2 \text{Re}[n_{\text{eff}}]}{\partial \lambda^2} \quad (1)$$

$$D_s(\lambda) = \frac{\partial D(\lambda)}{\partial \lambda} \quad (2)$$

$$L_c = 8.686k_0 \text{Im}(n_{\text{eff}}) \quad (3)$$

$$A_{\text{eff}} = \frac{2\pi \left(\int_0^\infty |E_a(r)|^2 r dr \right)^2}{\int_0^\infty |E_a(r)|^4 r dr} \quad (4)$$

$$\gamma = \frac{n_2 \omega}{c A_{\text{eff}}} = \frac{2\pi n_2}{\lambda A_{\text{eff}}} \quad (5)$$

where, c is the velocity of light in a vacuum, $\text{Re}(n_{\text{eff}})$ and $\text{Im}(n_{\text{eff}})$ are the real and imaginary parts of complex effective index n_{eff} , λ is the operating wavelength, E is the electric field, n_2 is the nonlinear refractive index coefficient and $k_0 = 2\pi/\lambda$ is the free space wave number.

Nonlinear Schrödinger equation (NLSE) was used for numerical calculation of SC spectrum [13, 15].

$$\frac{\partial A}{\partial z} + \frac{\alpha}{2} A + \frac{i}{2} \beta_2 \frac{\partial^2 A}{\partial T^2} - \frac{1}{6} \beta_3 \frac{\partial^3 A}{\partial T^3} = \quad (6)$$

$$i\gamma \left[|A|^2 A + i \frac{\lambda_c}{2\pi c} \frac{\partial}{\partial T} (|A|^2 A) - T_R A \frac{\partial |A|^2}{\partial T} \right]$$

where A is complex amplitude of the optical field, z is propagation distance, α is absorption coefficient of the fiber, λ_c is the center wavelength, T_R is the slope of the Raman gain and β_n with $n = 1$ to 3 are the n -th order propagation constant. T is defined as $T = t - z/v_g$ where t is the physical time and v_g is group velocity at the center wavelength.

STRUCTURE OF THE PROPOSED FIBER

A schematic cross section of the proposed seven air hole rings M-PCF is shown in Fig. 1. In the model, air hole diameter are kept identical at d , with the exception of air hole diameters of the first and fifth rings, which have diameter of d_1 and d_2 , respectively. Air hole diameter of the fifth ring d_2 is double the air hole diameter of the first ring d_1 , i.e. $d_2 = 2d_1$. Reductions in air hole diameters of the first and fifth rings, are due to difficulty in achieving

near zero flattened chromatic dispersion using a conventional holey fiber structure. Distance between respective air holes or its pitch is kept at Λ . Base material of the proposed holey fiber is made up of pure silica.

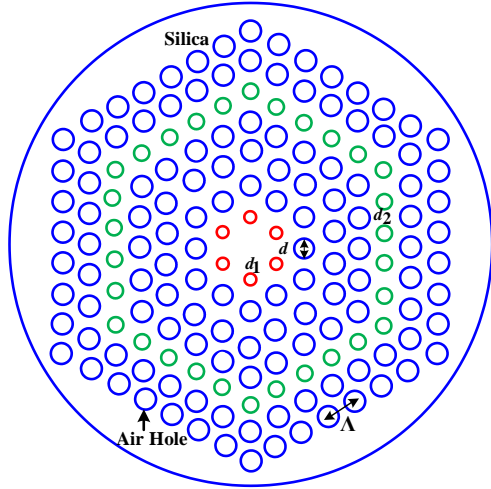
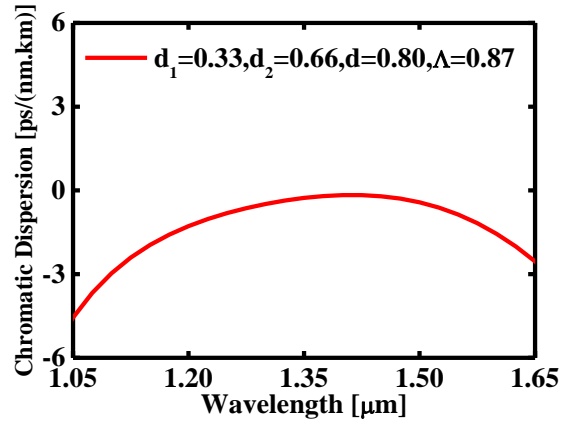


Figure 1 Proposed PCF with five rings of air hole with three different diameters d_1 , d_2 , d , and pitch Λ .

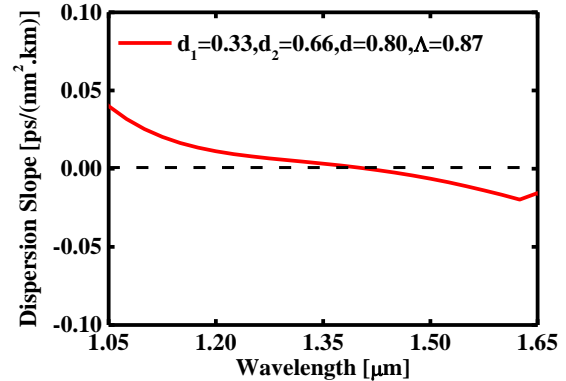
RESULTS AND DISCUSSION

For our numerical simulation, selected parameters are $d_1 = 0.33 \mu\text{m}$, $d_2 = 0.66 \mu\text{m}$, $d = 0.80 \mu\text{m}$ and $\Lambda = 0.87 \mu\text{m}$. Fig. 2 and Fig. 3 show different properties of the proposed fiber; chromatic dispersion (Fig. 2(a)), chromatic dispersion slope (Fig. 2(b)), confinement loss (Fig. 2(c)), effective area (Fig. 3(a)) and nonlinear coefficient properties (Fig. 3(b)), for different wavelength.

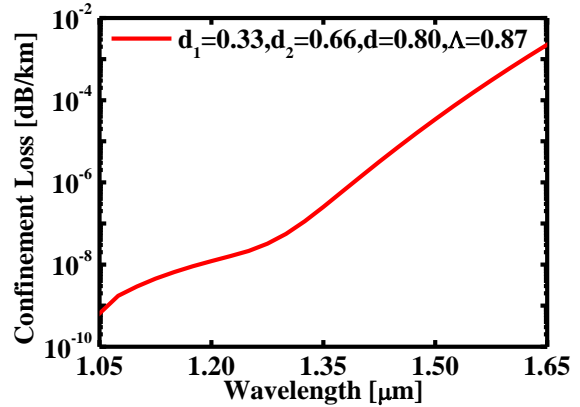
It can be seen that the proposed M-PCF exhibits an ultra-flattened chromatic dispersion of $0.0 \sim -4.5 \text{ ps}/(\text{nm}\cdot\text{km})$ in the observed wavelength range of $1.05 \mu\text{m}$ to $1.65 \mu\text{m}$. Moreover, confinement loss is kept low below $10^{-2} \text{ dB}/\text{km}$ at all observed wavelength range. Effective area of the proposed M-PCF is found to be $1.78 \mu\text{m}^2$, $2.08 \mu\text{m}^2$ and $2.42 \mu\text{m}^2$ at wavelengths of $1.06 \mu\text{m}$, $1.3 \mu\text{m}$ and $1.55 \mu\text{m}$ respectively. These are relatively smaller as compared to conventional fiber which commonly has an effective area of about $86 \mu\text{m}^2$ at $1.55 \mu\text{m}$ wavelength. The corresponding nonlinear coefficients are $104 \text{ W}^{-1}\text{km}^{-1}$, $72 \text{ W}^{-1}\text{km}^{-1}$ and $52 \text{ W}^{-1}\text{km}^{-1}$ at wavelength of $1.06 \mu\text{m}$, $1.30 \mu\text{m}$ and $1.55 \mu\text{m}$, respectively; comparatively higher than nonlinear coefficients of fibers reported in references [2-6].



(a)

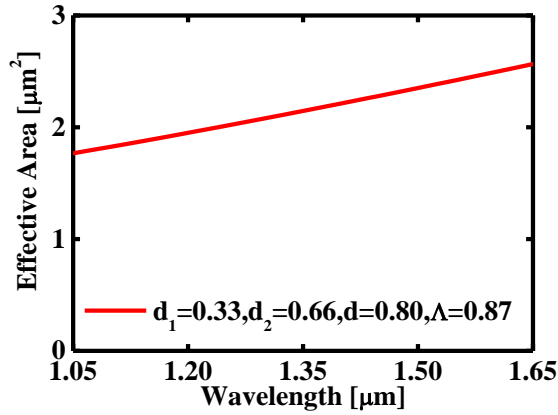


(b)

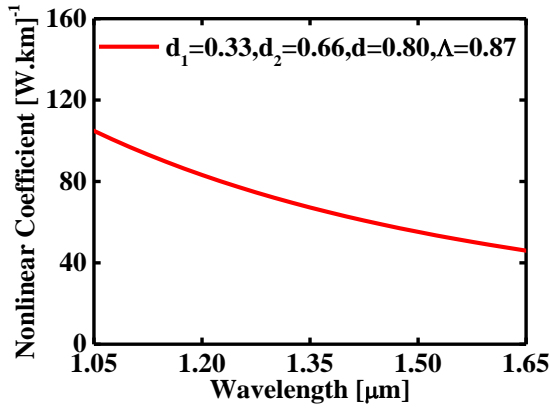


(c)

Figure 2: (a) chromatic dispersion, (b) chromatic dispersion slop and (c) confinement loss, of the proposed supercontinuum generated HN-PCF, for $\Lambda = 0.87 \mu\text{m}$, $d_1 = 0.33 \mu\text{m}$, $d_2 = 0.66 \mu\text{m}$ and $d = 0.80 \mu\text{m}$, at different wavelength.



(a)

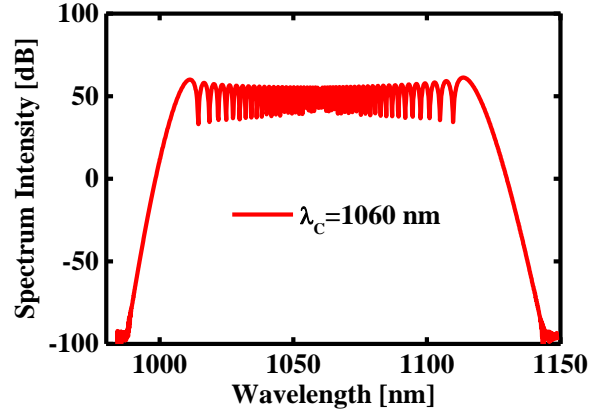


(b)

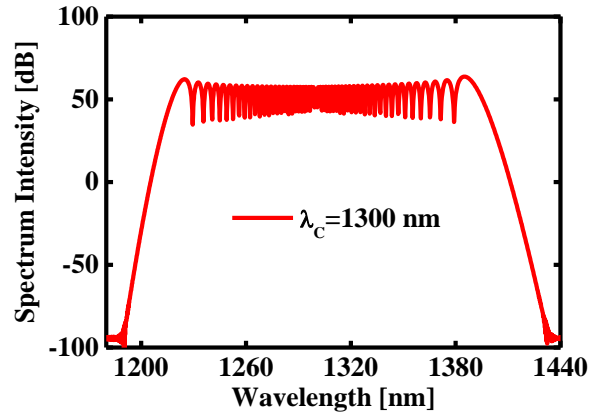
Figure 3: (a) effective area, and (b) nonlinear coefficient of the proposed supercontinuum generated HN-PCF, for $\Lambda = 0.87 \mu\text{m}$, $d_1 = 0.33 \mu\text{m}$, $d_2 = 0.66 \mu\text{m}$ and $d = 0.80 \mu\text{m}$, at different wavelength.

NLSE was used for numerical calculation of SC spectrum [13, 15], which was solved by split-step Fourier method. SC spectrum in the proposed M-PCF was numerically calculated at 1.06 μm , 1.30 μm and 1.55 μm center wavelengths which are shown in Fig. 4 (a), (b) and (c), respectively. Propagation of the sech^2 waveform with full width at half maximum (FWHM), T_{FWHM} of 1.0 ps and Raman scattering parameter T_R of 3.0 fs through the proposed M-PCF was considered. Propagation constants β_2 and β_3 , around the carrier frequency are shown in Table I at center wavelengths of $\lambda_c = 1.06 \mu\text{m}$, $\lambda_c = 1.30 \mu\text{m}$ and $\lambda_c = 1.55 \mu\text{m}$. After numerical simulation, the incident pulse input power P_{in} and fiber length L_F were obtained which are shown in Table I. The achieved input powers are 1.6 kW at 1.06 μm center wavelength, 2.4 kW at 1.30 μm center wavelength and 3.8 kW at 1.55 μm center wavelength;

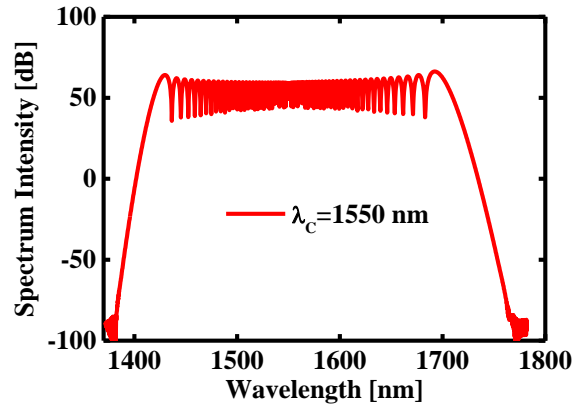
with acquired fiber length L_F of 6 m for all center wavelengths considered. These P_{in} values are higher and L_F values are lower than those reported light sources in references [7-13].



(a)



(b)



(c)

Figure 4: Spectrum intensity of the proposed supercontinuum generated HN-PCF at center wavelengths of (a) 1.06 μm , (b) 1.30 μm and (c) 1.55 μm .

Table I. Fiber parameters.

Parameters	$\lambda_c=1.06$ [μm]	$\lambda_c=1.30$ [μm]	$\lambda_c=1.55$ [μm]
β_2 [ps^2/km]	2.98	0.318	2.29
β_3 [ps^3/km]	0.01	0.0045	-0.0036
P_{in} [kW]	1.6	2.4	3.8
L_F [m]	6.0	6.0	6.0

CONCLUSION

It has been shown that the proposed M-PCF has high nonlinear coefficient with ultra-flattened chromatic dispersion and very low confinement loss, in the wavelength range of 1.05 μm to 1.65 μm . Moreover, the proposed M-PCF provides high longitudinal resolution and high power at 1.06 μm , 1.30 μm and 1.55 μm center wavelengths, with short fiber length of 6 m in all center wavelengths considered. These characteristics suggest that the proposed M-PCF may be suitable for optical communications and supercontinuum generation applications, including medical imaging, tunable wavelength conversion and optical studies of photonic devices.

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